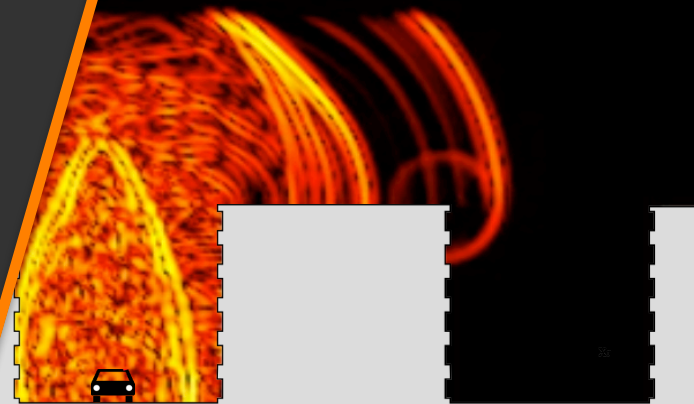


# Wave-based modelling in the built environment using the PSTD method: developments and prospects

Maarten Hornikx

07-07-2015



**TU/e**

Technische Universiteit  
**Eindhoven**  
University of Technology

# Short bio



1998 - 2004

**M.Sc.** Architecture, Building and Planning  
Eindhoven University of Technology



2004 - 2009

**Ph.D.** in Applied Acoustics,  
Chalmers University of Technology, Göteborg



2007

University of Mississippi  
National Center for Physical Acoustics



2009 - 2011

**Post-Doc** Aero-Acoustics  
KU Leuven Individual Marie-Curie IEF fellowship



2011 - 2013

**Senior Researcher** position Applied Acoustics,  
Chalmers University of Technology, Göteborg



2012- ...

**Assistant Professor** in Building Acoustics,  
Dept. of the Built Environment  
Eindhoven University of Technology

# TU/e Building Acoustics chair

4 Units

AUDE: Architectural Urban Design and Engineering

BPS: Building Physics and Services

SD: Structural Design

USS: Urban Science & Systems

1 Bachelor program

2 Master's programs

- Master Architecture, Building and Planning
- Master Construction Management and Engineering



# Building Physics and Services

6 Research groups

Building Acoustics

Building Lighting

Building Materials

Building Physics

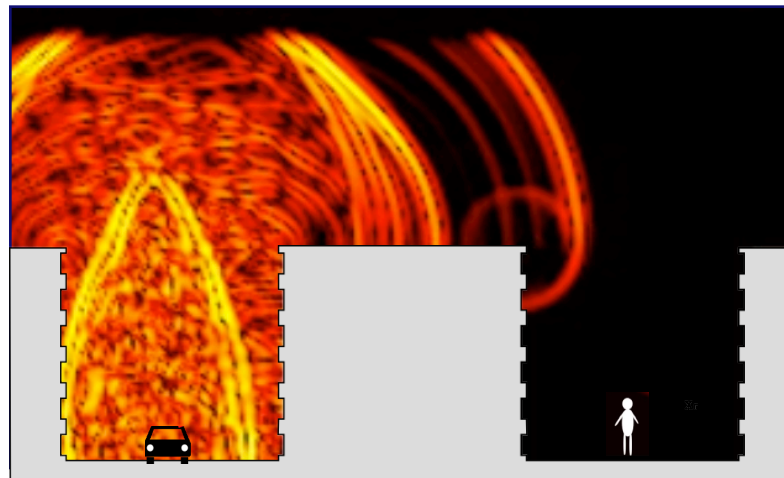
Building Performance

Building Services





# TU/e Building Acoustics chair



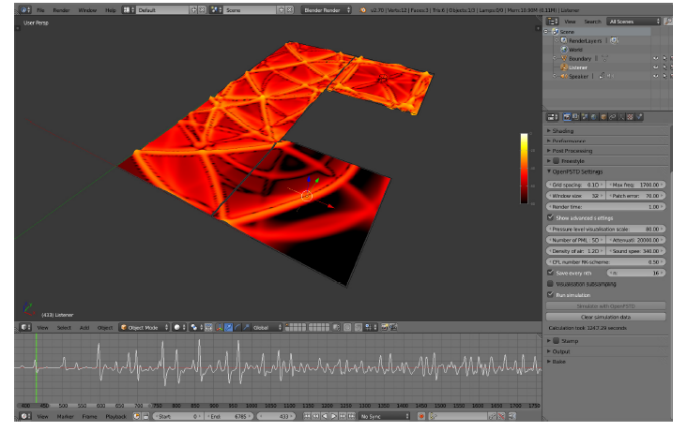
# TU/e Building Acoustics chair

## Urban Acoustics

Computational methods

Urban propagation effects

Human echolocation



## Room and Building Acoustics

Experimental methods

Computational methods

Concert hall and theatre acoustics

Healthy environments

Lightweight structures



# TU/e Building Acoustics chair



Maarten Hornikx



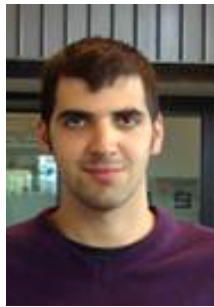
Constant Hak



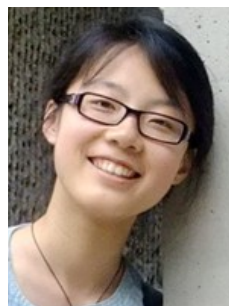
Remy Wenmaekers



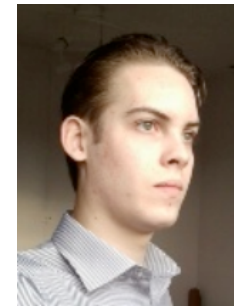
Raúl Pagán



Fotis Georgiou



Chang Liu



Rick de Vos



Michiel Fortuin



Qin Yi\*\*



Ella Braat-Eggen



Indra Sihar



Jikke Reinten



Omar Richardson



Louis van Harten

\*\* From 9/2015

# Research vision

We must aim for a high acoustic quality in the built environment at all times, and it must be free from adverse health effects due to noise.

To support this aim, my research is devoted to

- Development of prediction methods to study (fundamental) acoustics and auditory perception of the built environment;
- Using these tools to integrate and optimize acoustics for a sustainable (re)design of the built environment and technical innovations therein.

# Research vision

**Challenges:** Tackle major contemporary problems in acoustics

- Urban noise problem



- Low frequency acoustics related to lightweight buildings



[www.sustainabilitymatters.net.au](http://www.sustainabilitymatters.net.au)



[www.smstimmerframe.co.uk](http://www.smstimmerframe.co.uk)



# Research vision

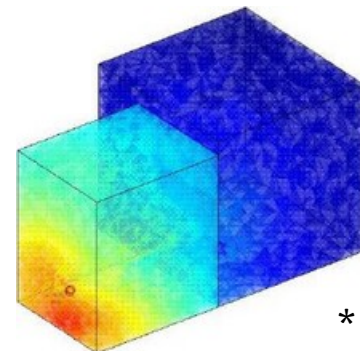
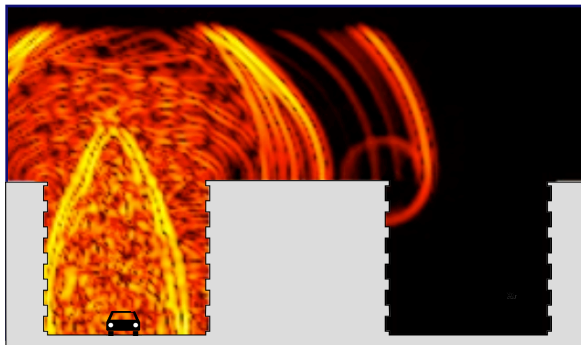
## Challenges: Tools

- Design of acoustically realistic Virtual Reality systems



<http://www.techmania.nl>

- Development and application of open source acoustic prediction methods



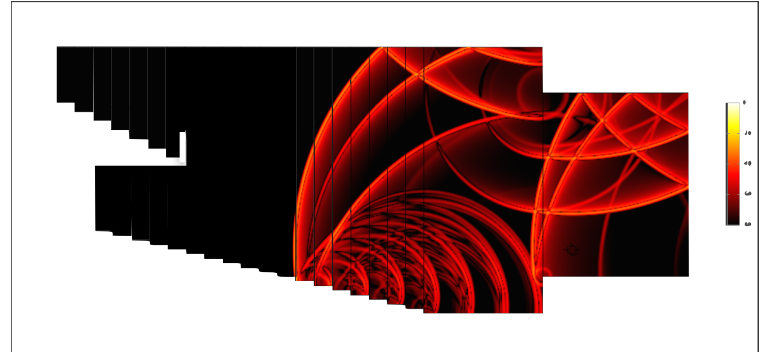
\*

\*Y. Jing, N. Xiang, On the use of a diffusion equation model for sound energy flow prediction in acoustically coupled spaces, in Proc. of the COMSOL Conference 2008 Boston



# Research agenda

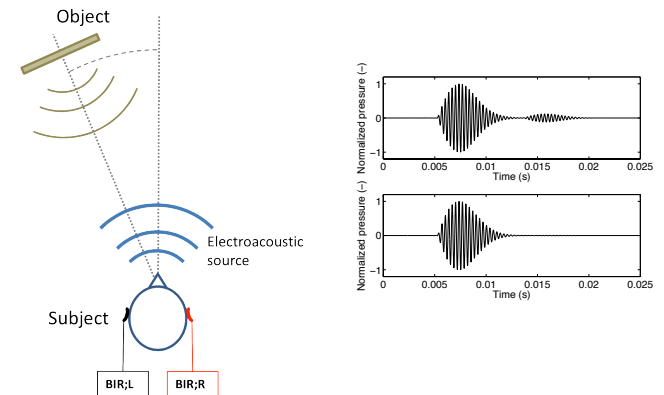
Computational methods



Propagation effects / noise mitigation

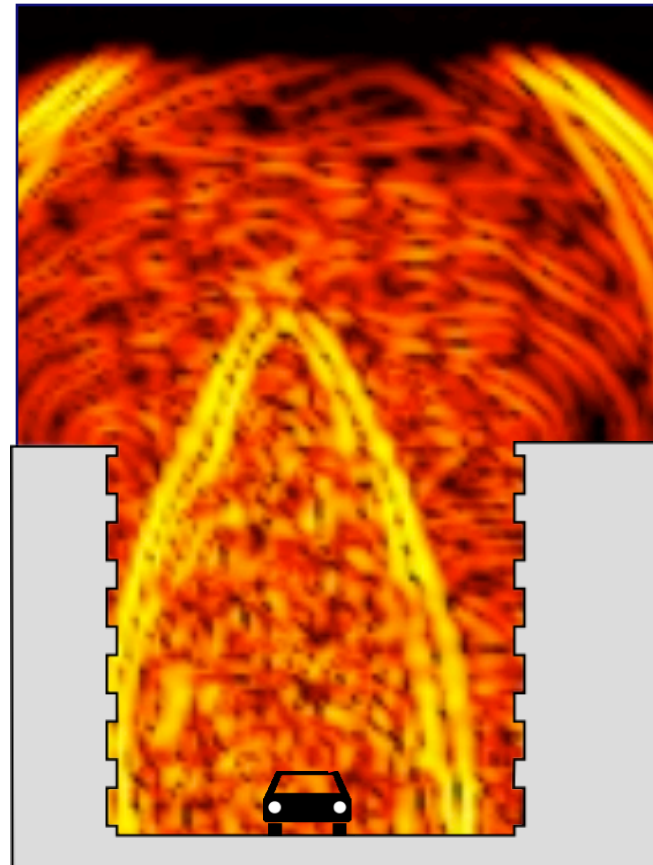


Human echolocation / auralization



openPSTD

Marie-Curie CIG grant: 2012-2016

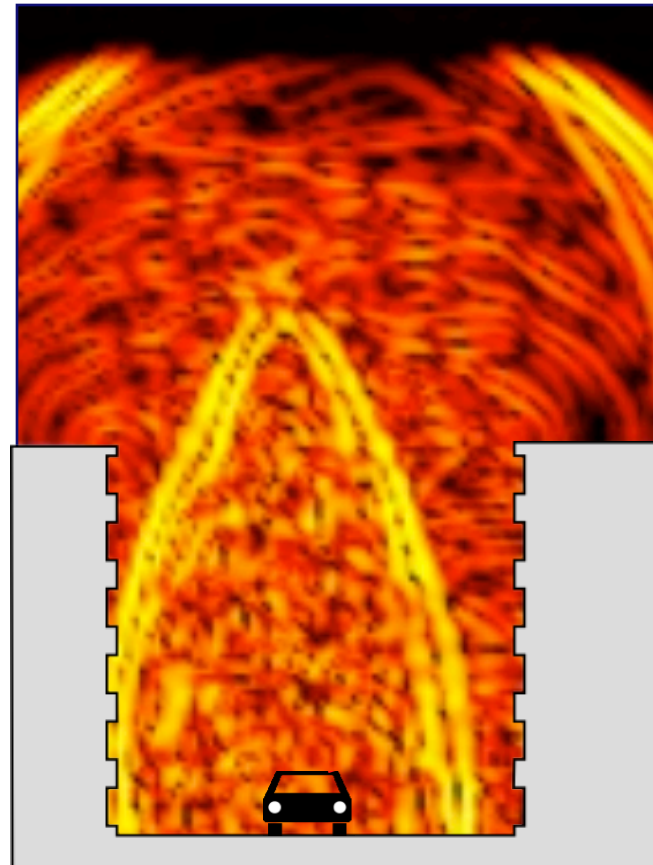


# Introduction

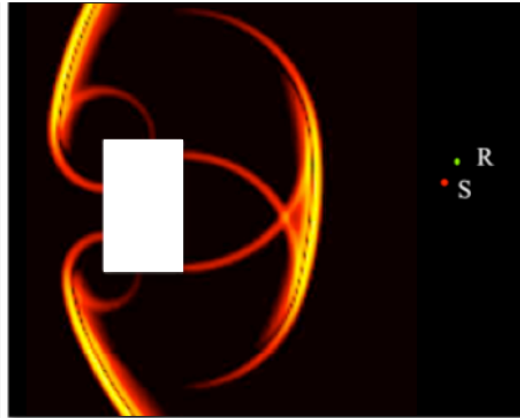
Scope: Modelling of indoor and outdoor acoustic scenarios where wave effects are important

- Meteorological effects
- Complex geometries (including curved surfaces)
- Geometrically shielded environments
- Explicitly modelling of boundary media
- Interference effects (low frequencies)

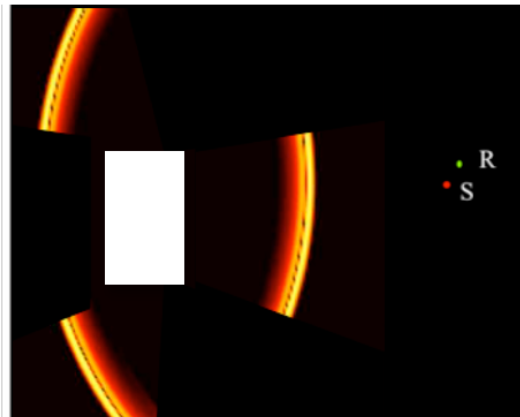
-> **Wave-based acoustics**



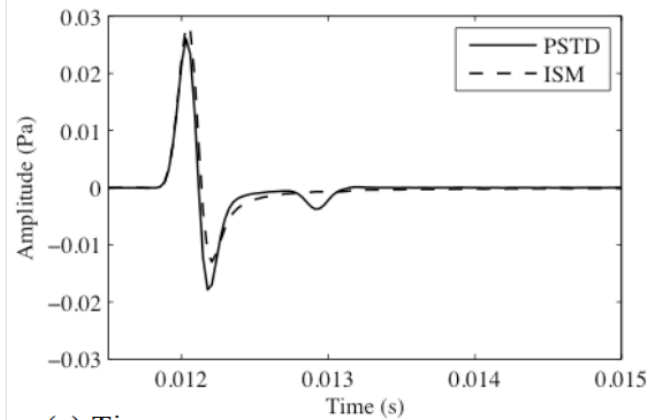
# Introduction



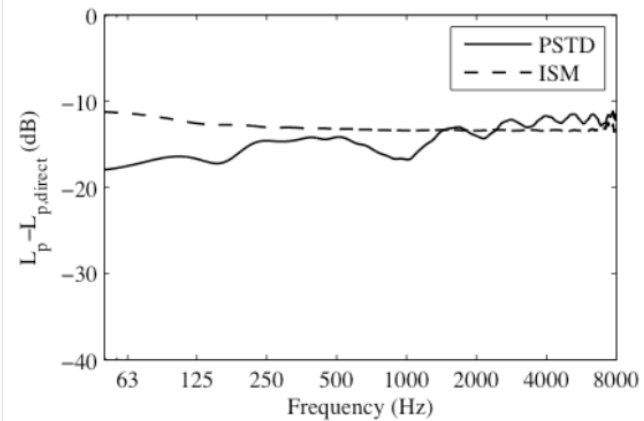
(a) PSTD



(b) ISM



(c) Time responses

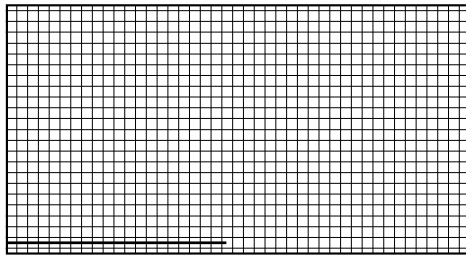


(d) Frequency spectra

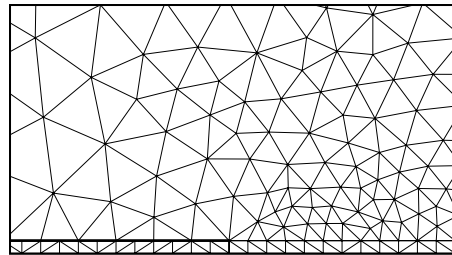
# Introduction

Solution methods wave-based acoustics (see<sup>1</sup> for references)

- Finite Element Method (mesh (b)) (FEM)
- Discontinuous Galerkin method (mesh (b)) (DG)
- Finite-Difference Time-Domain method (mesh (a)) (FDTD)
- Pseudo-Spectral Time-Domain method (mesh (a)) (PSTD)



(a)



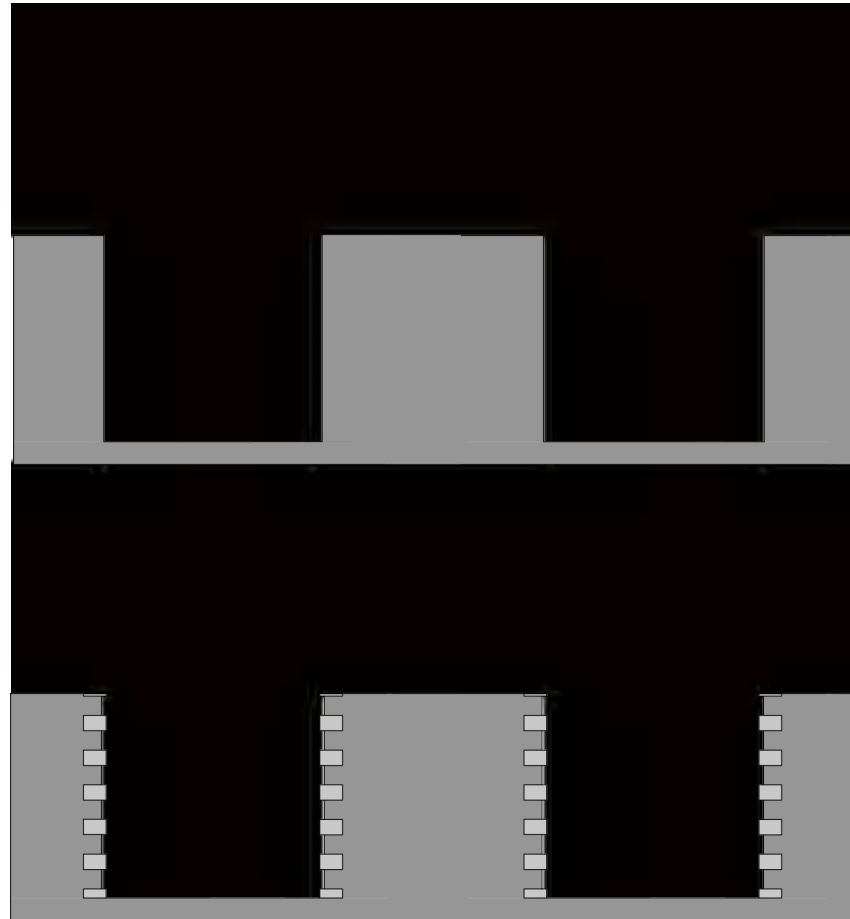
(b)

**Challenge: efficient wave-based acoustic method**

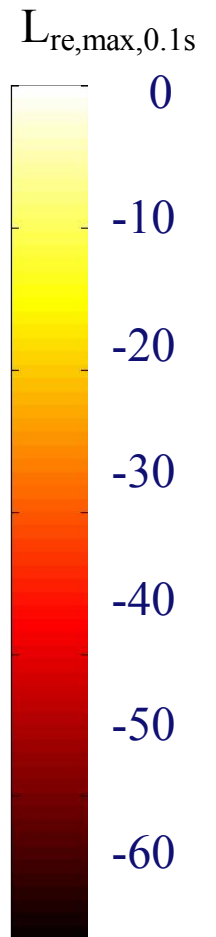
PSTD is most efficient method, but some developments are left to utilize its efficiency for generic situations

<sup>1</sup>Hornikx, M. Numerical modeling of sound propagation to closed urban courtyards. (2009). ISBN 978-91-7385-298-2. Department of Civil and Environmental Engineering, Division of Applied Acoustics, Vibroacoustics Group, Chalmers University of Technology, Sweden.

Flat facades



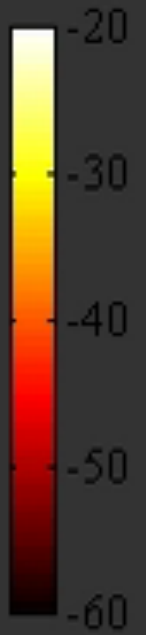
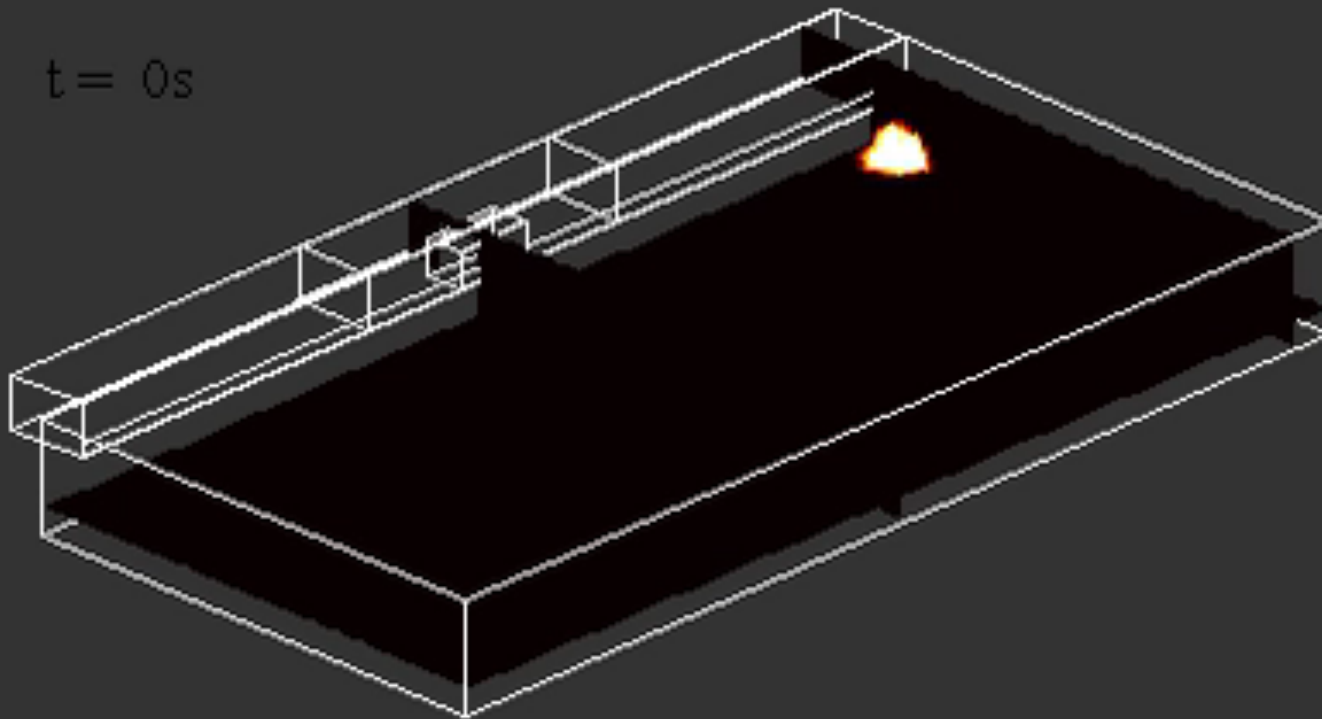
Profiled facades





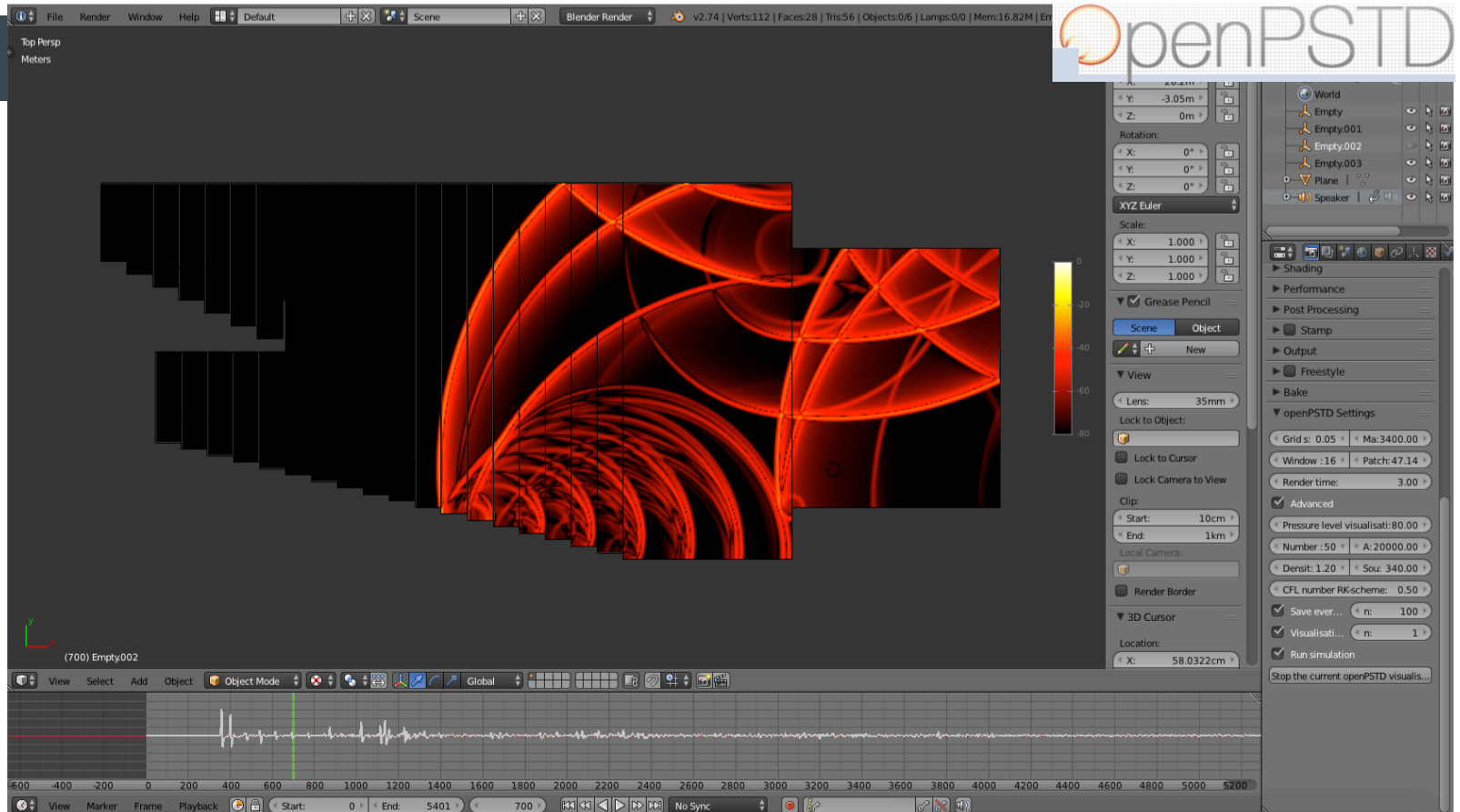
# openPSTD

$t = 0s$



# openPSTD

[www.openpstd.org](http://www.openpstd.org)

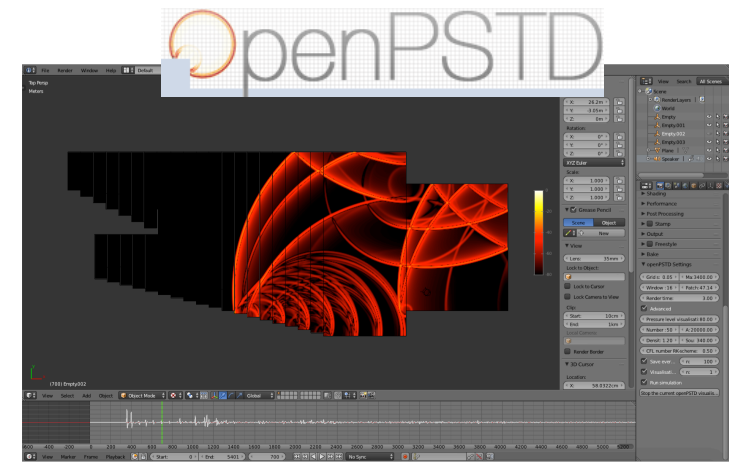


Krijnen, T., Hornikx, M. (2014). openPSTD: the open source implementation of the Pseudo Spectral Time-Domain method, Forum Acusticum, 7-12 September 2014, Krakow, Poland.

Maarten Hornikx

## openPSTD v1.0

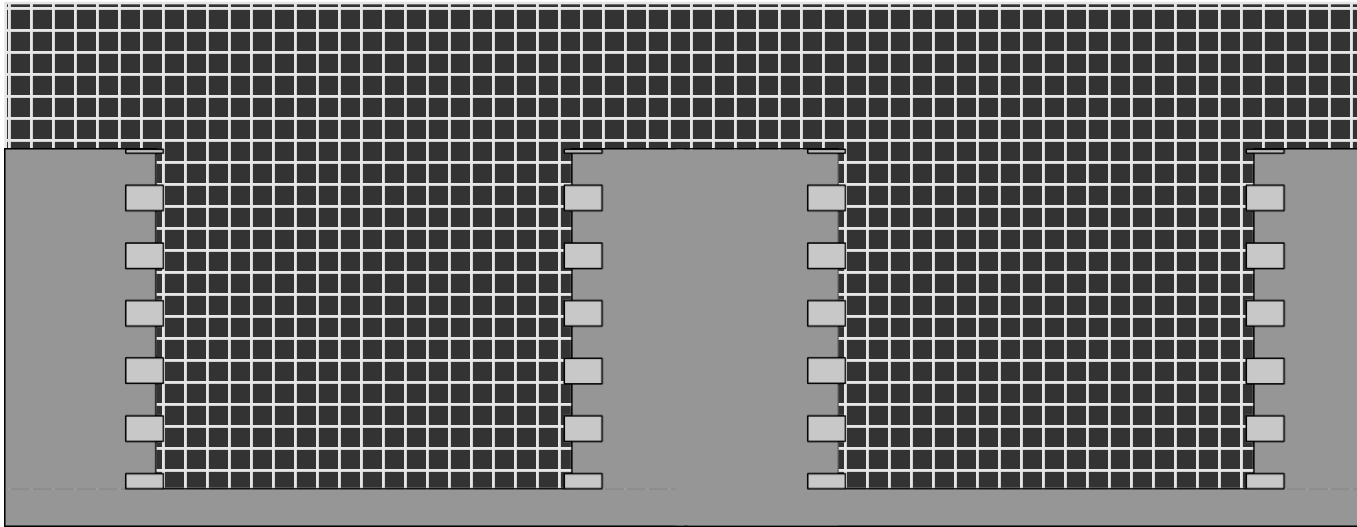
- 2D implementation
- Boundaries with real valued frequency independent impedance values
- Computation of impulse responses
- Postprocessing with program of your choice (Matlab, Python...)
- GPU acceleration



# Developments

## PSTD method, mesh

Cartesian grid, solution sought at all grid points



- Example: 3D environment: 180m x 63m x 40m,  $f_{upper} = 500$  Hz  
PSTD:  $\Delta x = 0.32$  m, around  $14 \cdot 10^6$  computational cells  
**Compare with**  
FDTD:  $\Delta x = 0.06$  m, around  $1.75 \cdot 10^9$  computational cells

# Developments

## PSTD method, time-derivative

- The linearized Euler equations (LEE)

$$\frac{\partial p'}{\partial t} = -\rho_0 c^2 \nabla \mathbf{u}' \cdot (\mathbf{u}_0 \cdot \nabla) p'$$

$$\frac{\partial \mathbf{u}'}{\partial t} = -(\mathbf{u}' \cdot \nabla) \mathbf{u}_0 - (\mathbf{u}_0 \cdot \nabla) \mathbf{u}' - \frac{1}{\rho_0} \nabla p'$$

$$\frac{\partial \mathbf{q}'}{\partial t} = -L \mathbf{q}'$$

$$\mathbf{q}' = \begin{bmatrix} p' & u'_x & u'_y & u'_z \end{bmatrix}^T$$

- Time-derivative with explicit low-storage 6-stage Runge-Kutta (RKo6s) method\*

$$\mathbf{q}'(\mathbf{x}, t_0) = \mathbf{q}'(\mathbf{x}, t)$$

$$\mathbf{q}'(\mathbf{x}, t_i) \approx \mathbf{q}'(\mathbf{x}, t_0) - \gamma_i \Delta t (L \mathbf{q}'(\mathbf{x}, t_{i-1}))$$

$$\text{for } i = 1 \dots 6,$$

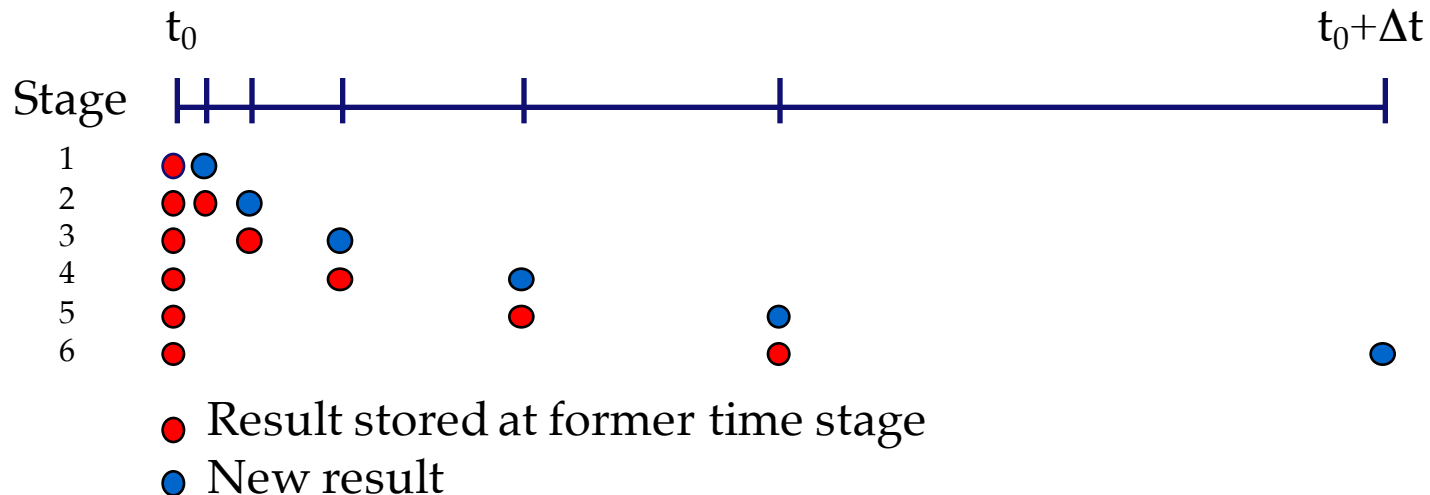
$$\mathbf{q}'(\mathbf{x}, t + \Delta t) \approx \mathbf{q}'(\mathbf{x}, t_6)$$

\*Bogey, C., Bailly, C., A family of low dispersive and low dissipative explicit schemes for flow and noise computation," J. Comput. Phys. 194, 194–214 (2004).

# Developments

## PSTD method, time-derivative

- Time-derivative with Runge-Kutta (RKO6s) method\*
- Explicit -> no matrix inversion
  - Efficient but more sensitive to stability than implicit schemes
- Multistage method (6 stages), but low storage capacity: only 2 former stage needs to be stored



\*Bogey, C., Bailly, C., A family of low dispersive and low dissipative explicit schemes for flow and noise computation," J. Comput. Phys. 194, 194–214 (2004).



# Developments

## PSTD method, spatial derivatives

- The linearized Euler equations (LEE)

$$\frac{\partial p'}{\partial t} = -\rho_0 c^2 \nabla \mathbf{u}' \cdot (\mathbf{u}_0 \cdot \nabla) p'$$

$$\frac{\partial \mathbf{u}'}{\partial t} = -(\mathbf{u}' \cdot \nabla) \mathbf{u}_0 - (\mathbf{u}_0 \cdot \nabla) \mathbf{u}' - \frac{1}{\rho_0} \nabla p'$$

$$\frac{\partial \mathbf{q}'}{\partial t} = -L \mathbf{q}'$$

$$\mathbf{q}' = \begin{bmatrix} p' & u'_x & u'_y & u'_z \end{bmatrix}^T$$

- Extended Fourier pseudospectral method\* to solve  $L \mathbf{q}'$

\*Hornikx, M., Waxler, R., Forssén, J., (2010). The extended Fourier pseudospectral time-domain method for atmospheric sound propagation, J. Acoust. Soc. Am., 128(4), 1632-1646.

# Developments

## PSTD method, spatial derivatives

- Example for  $dp/dx$  (1D Fourier transforms)

$$\left. \frac{\partial p}{\partial x} \right|_{n\Delta x} = F_x^{-1} \left( jk_x F_x [p] \right)$$

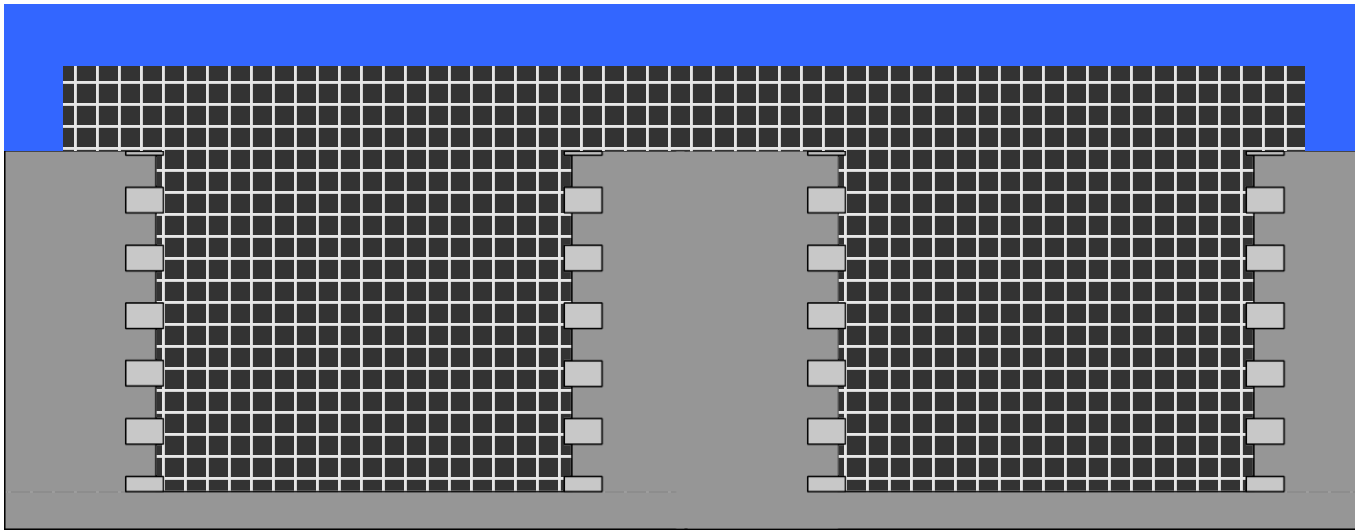
### Consequences of PSTD method

- Acoustic variables should spatially be periodic
- Spectral accuracy down to 2 spatial points ( $\Delta x$ ) per wavelength

# Developments

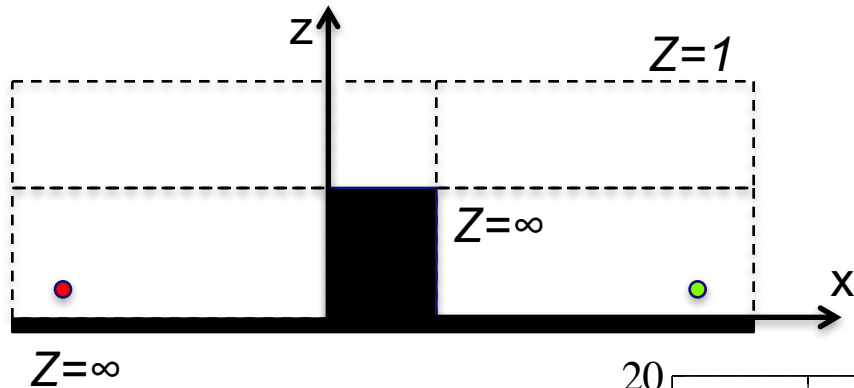
## PSTD method, mesh

- Non-reflecting boundaries modelled by an absorbing layer (PML)
- Materials modelled by a media with different densities
- Acoustic source (initial values or source function) and receiver positions assigned



# Developments

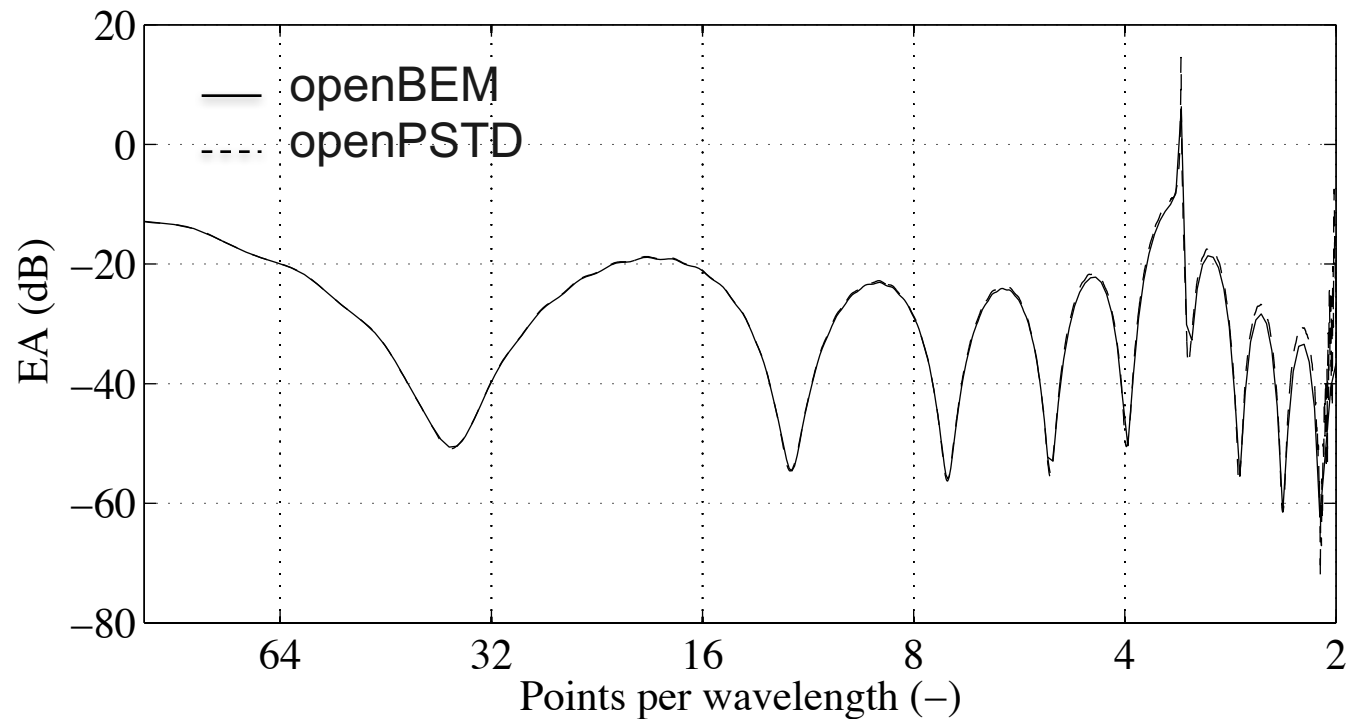
## Subdomains



$$(x_{\text{source}}, z_{\text{source}}) = (-10 \text{ m}, 1 \text{ m})$$

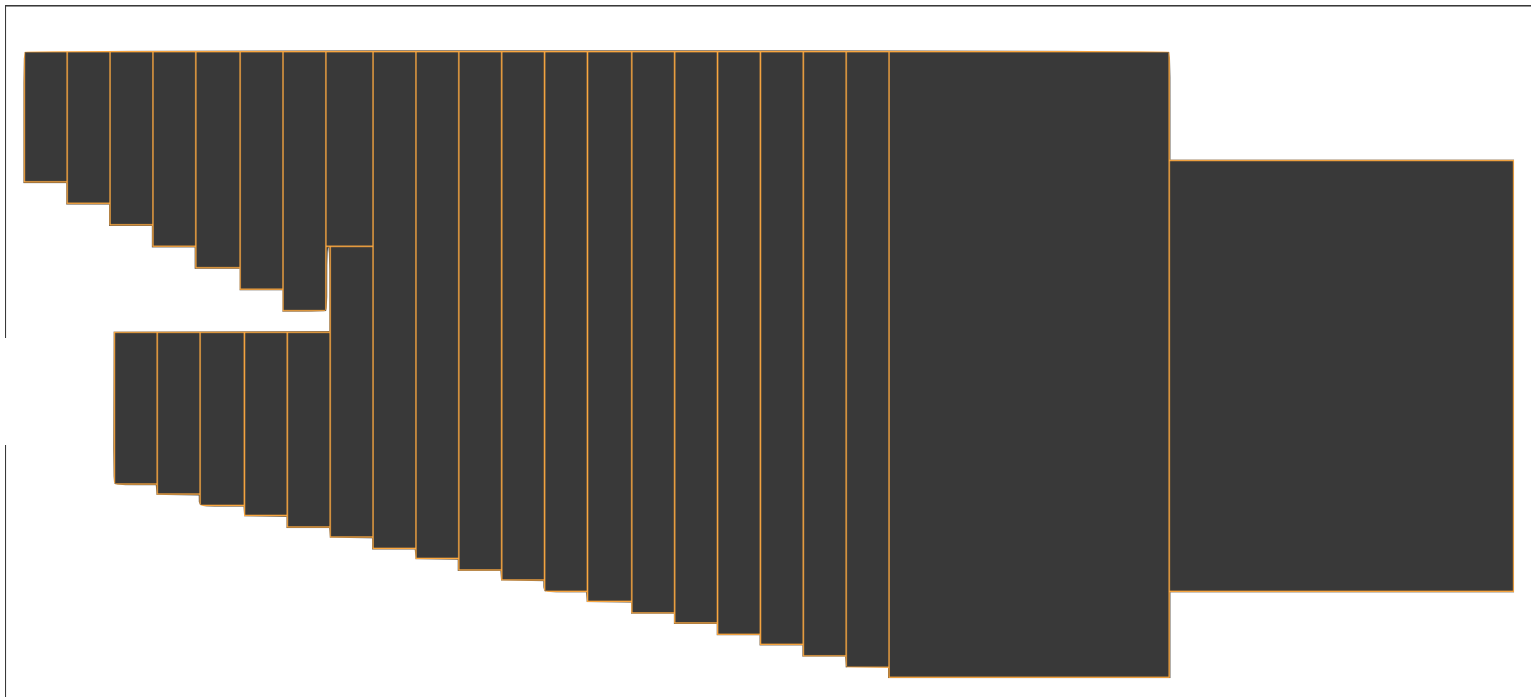
$$(x_{\text{rec}}, z_{\text{rec}}) = (14 \text{ m}, 1 \text{ m})$$

Barrier, 4 m wide, 5 m tall



## Subdomains

Domain decomposition



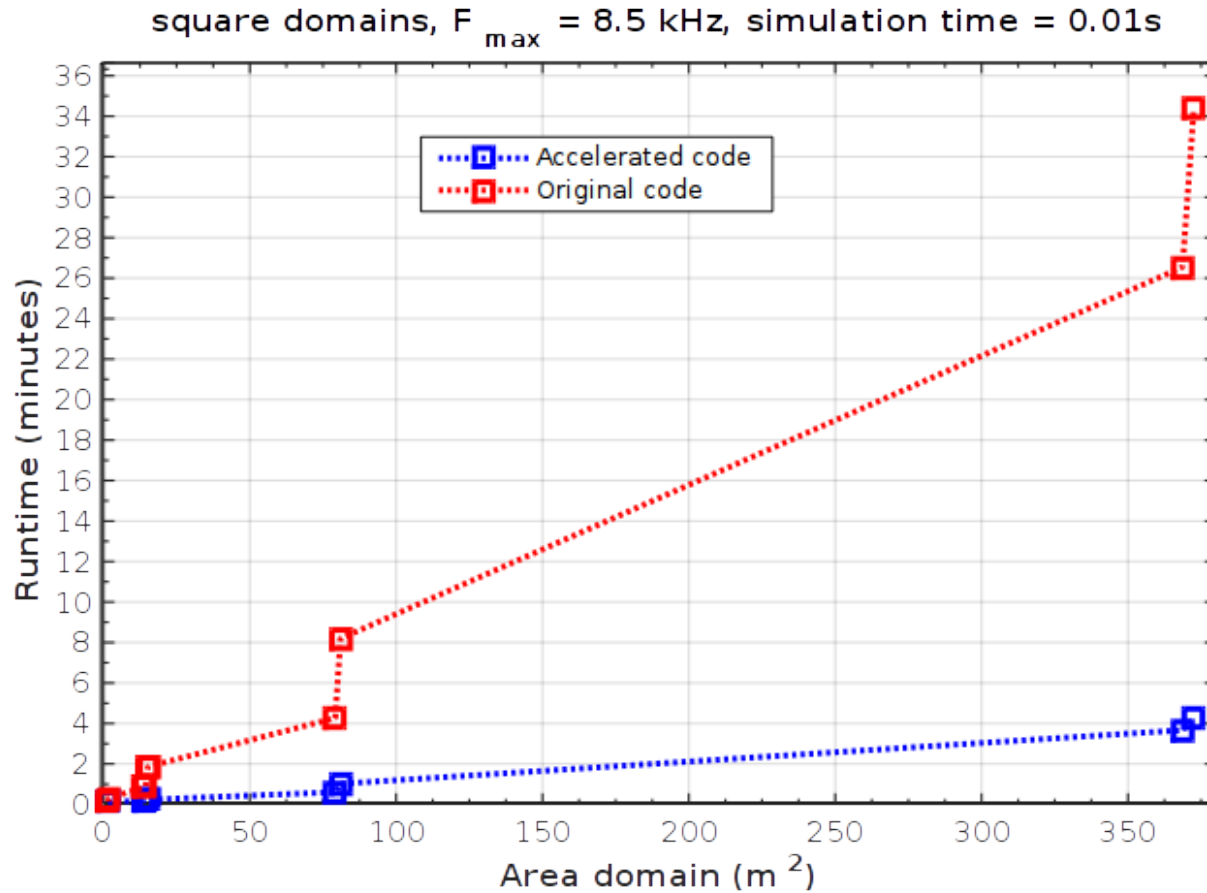
# Developments

## GPU acceleration



# Developments

## GPU acceleration

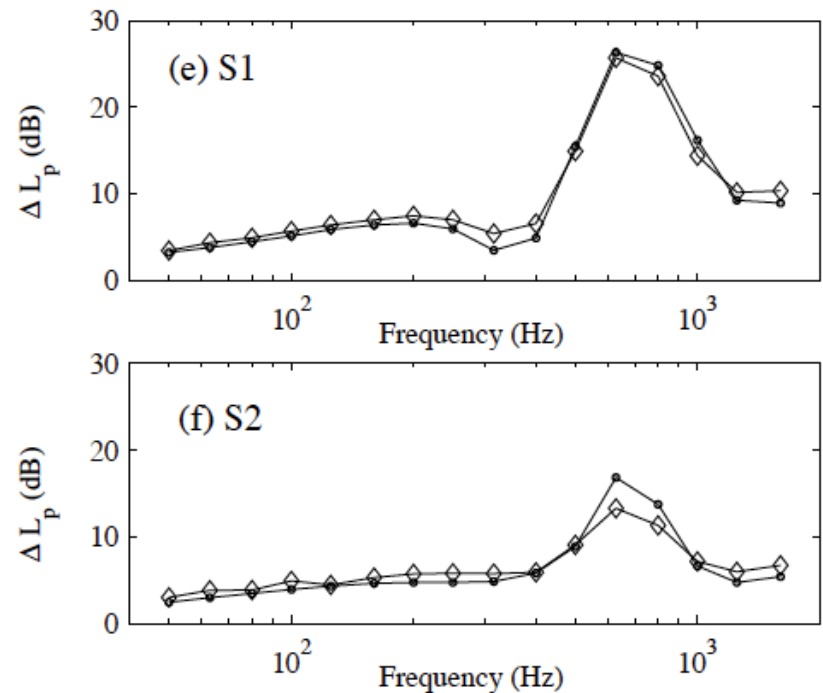
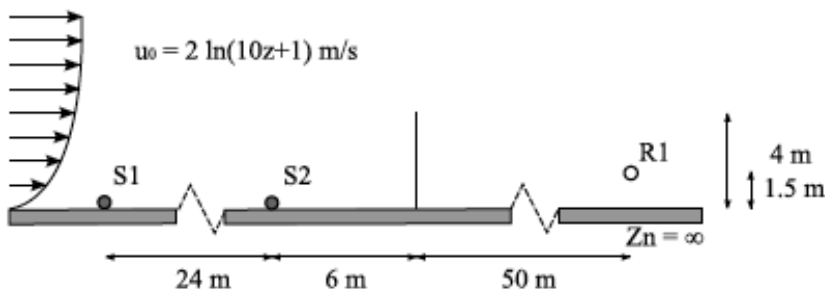


Louis van Harten

# Developments

## Boundaries and inhomogeneous moving medium

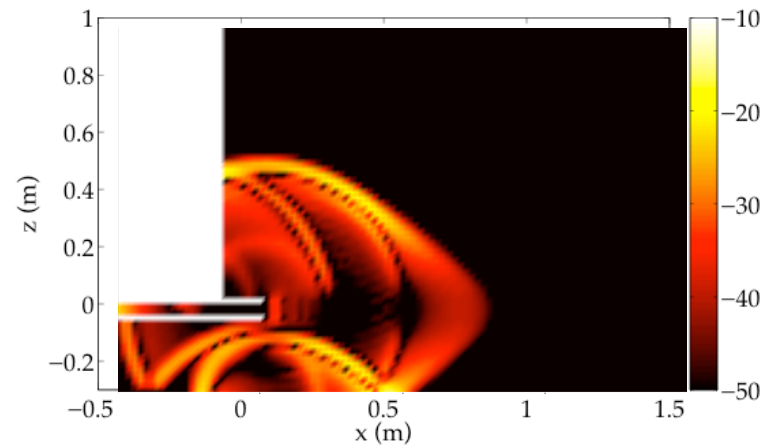
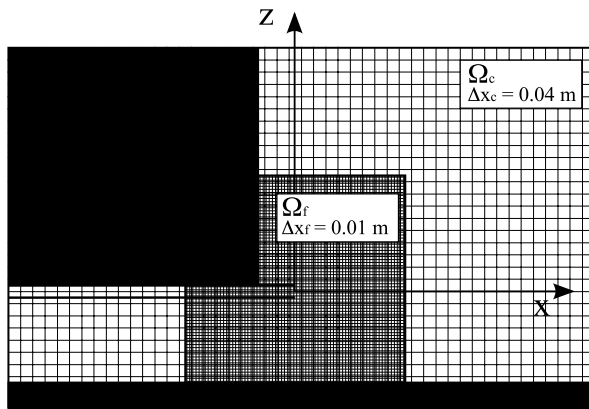
- Downward refraction due to wind or temperature gradients



Diamonds: PE method;  
Open circles: extended Fourier PSTD method

# Developments

## Local grid refinement

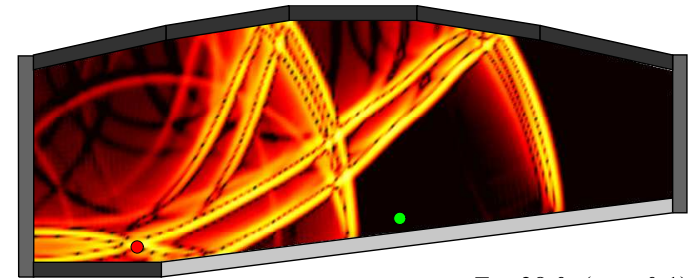
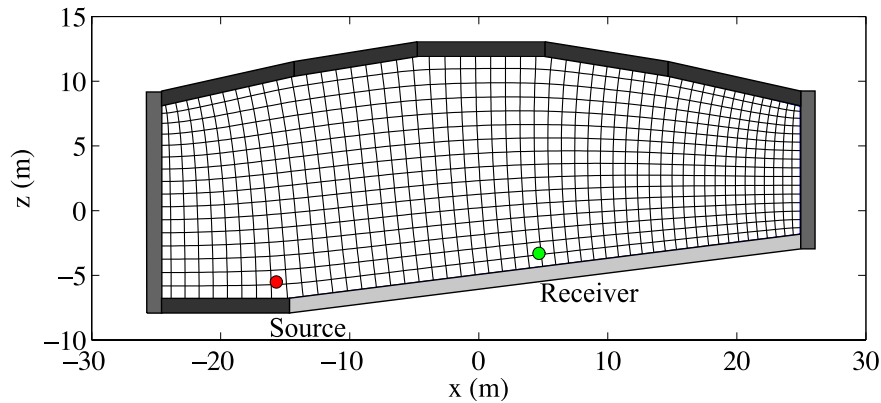


Hornikx, M., De Roeck, W., Desmet, W. (2012). A multi-domain Fourier pseudospectral time-domain method for the linearized Euler equations. *J. Comp. Phys.*, **231**(14), 4759-4774.

Hornikx, M., De Roeck, W., Toulorge, T., Desmet, W. (2015). Flow and geometrical effects on radiated noise from exhaust pipes computed by the Fourier pseudospectral time-domain method, *Computers and Fluids*, 116, 176-191.

# Developments

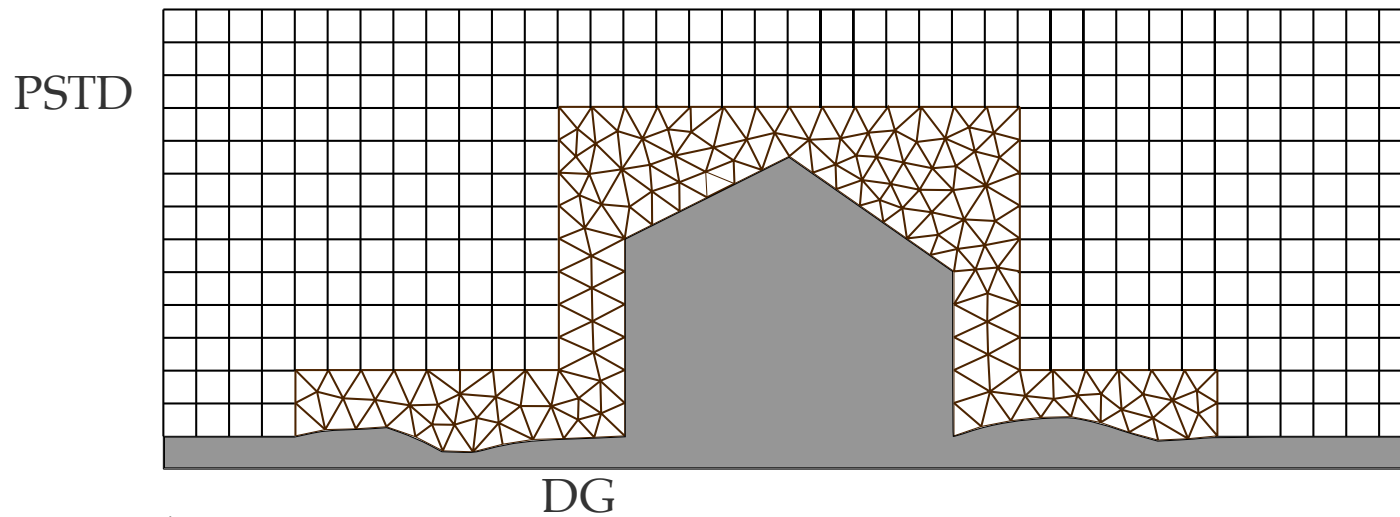
## Curvilinear implementation



- $Z = 38.0$  ( $\alpha_n = 0.1$ )
- $Z = 11.2$  ( $\alpha_n = 0.3$ )
- $Z = 2.6$  ( $\alpha_n = 0.8$ )
- $\Delta = 0.2$  m

# Developments

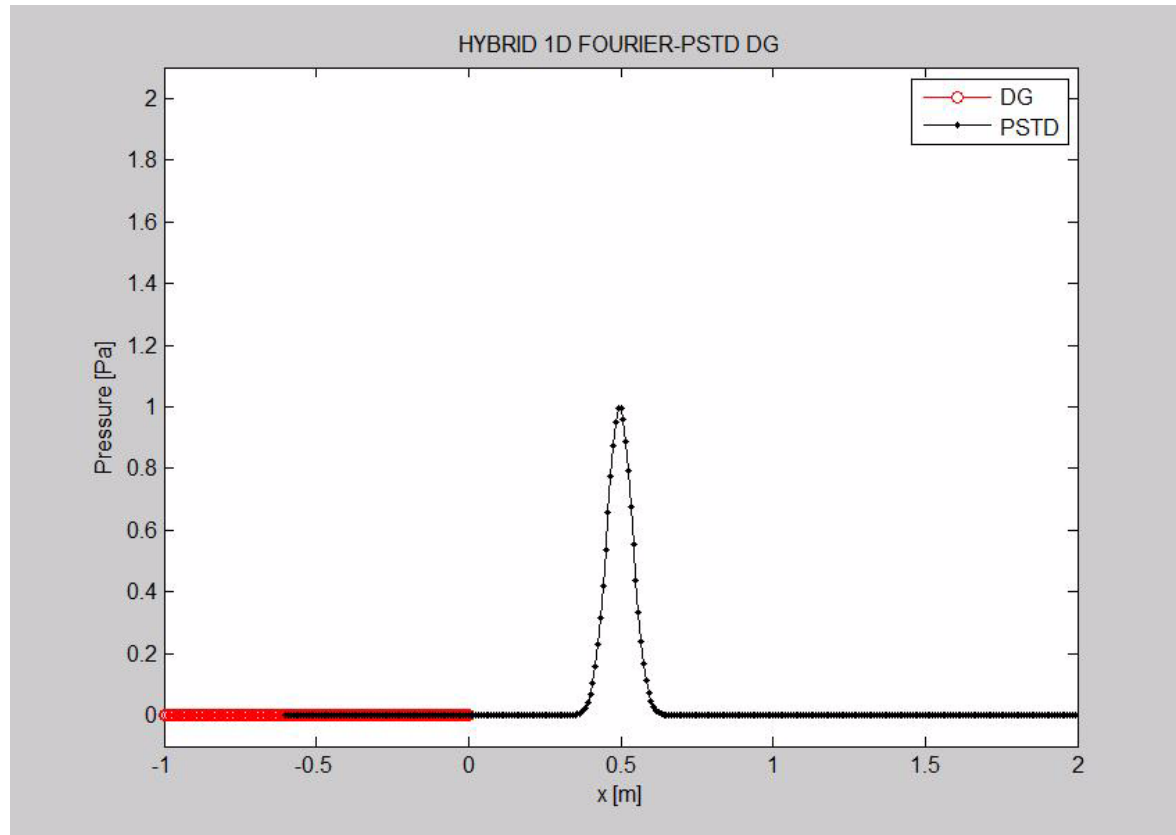
## Hybrid method



# Developments

## Hybrid method

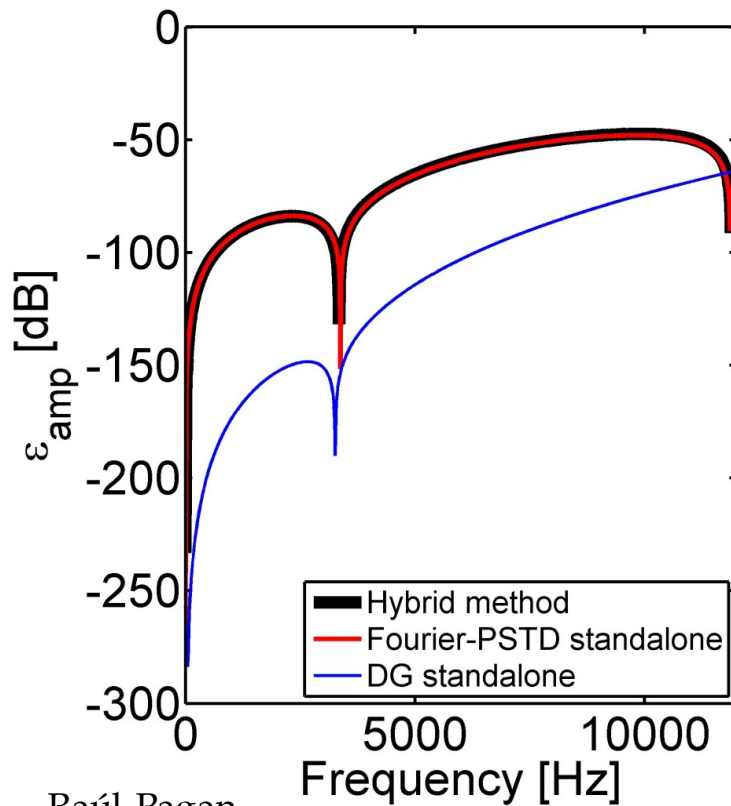
1D hybrid Fourier-PSTD and Discontinuous Galerkin implementation



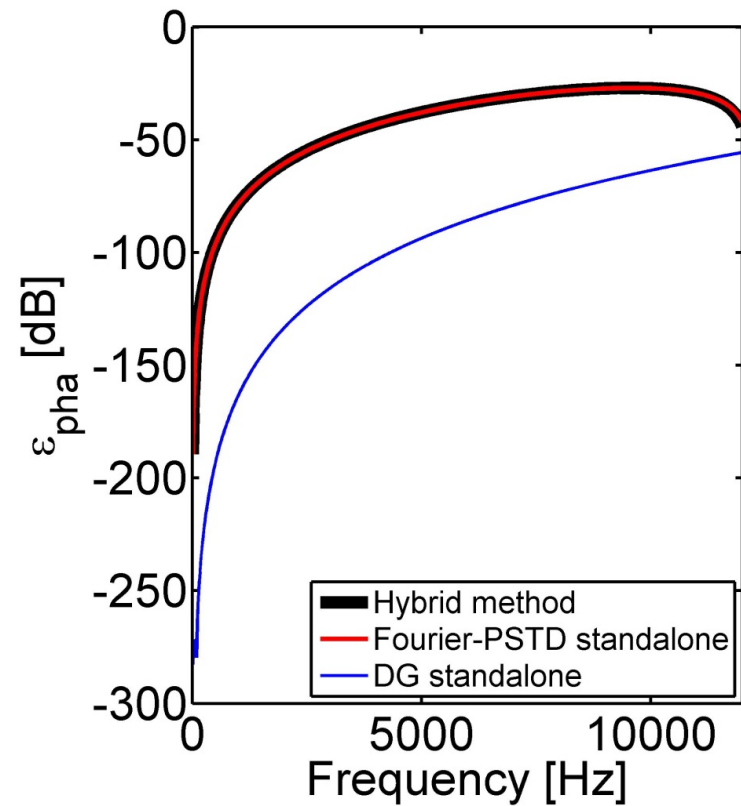
Raúl Pagan

## Hybrid method

Errors analysis hybrid PSTD-DG method



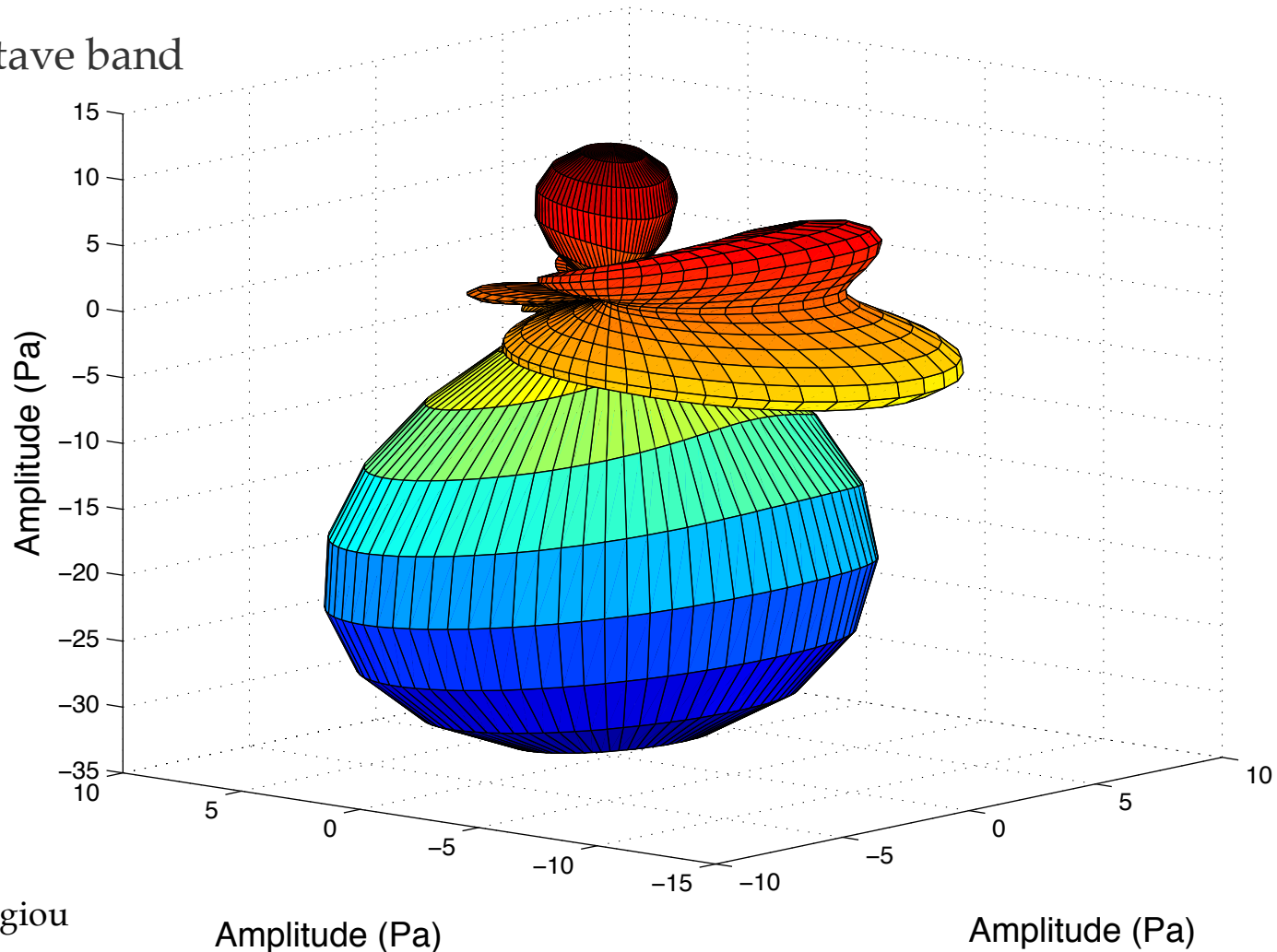
Raúl Pagan



# Developments

## Source directivity method

63 Hz octave band

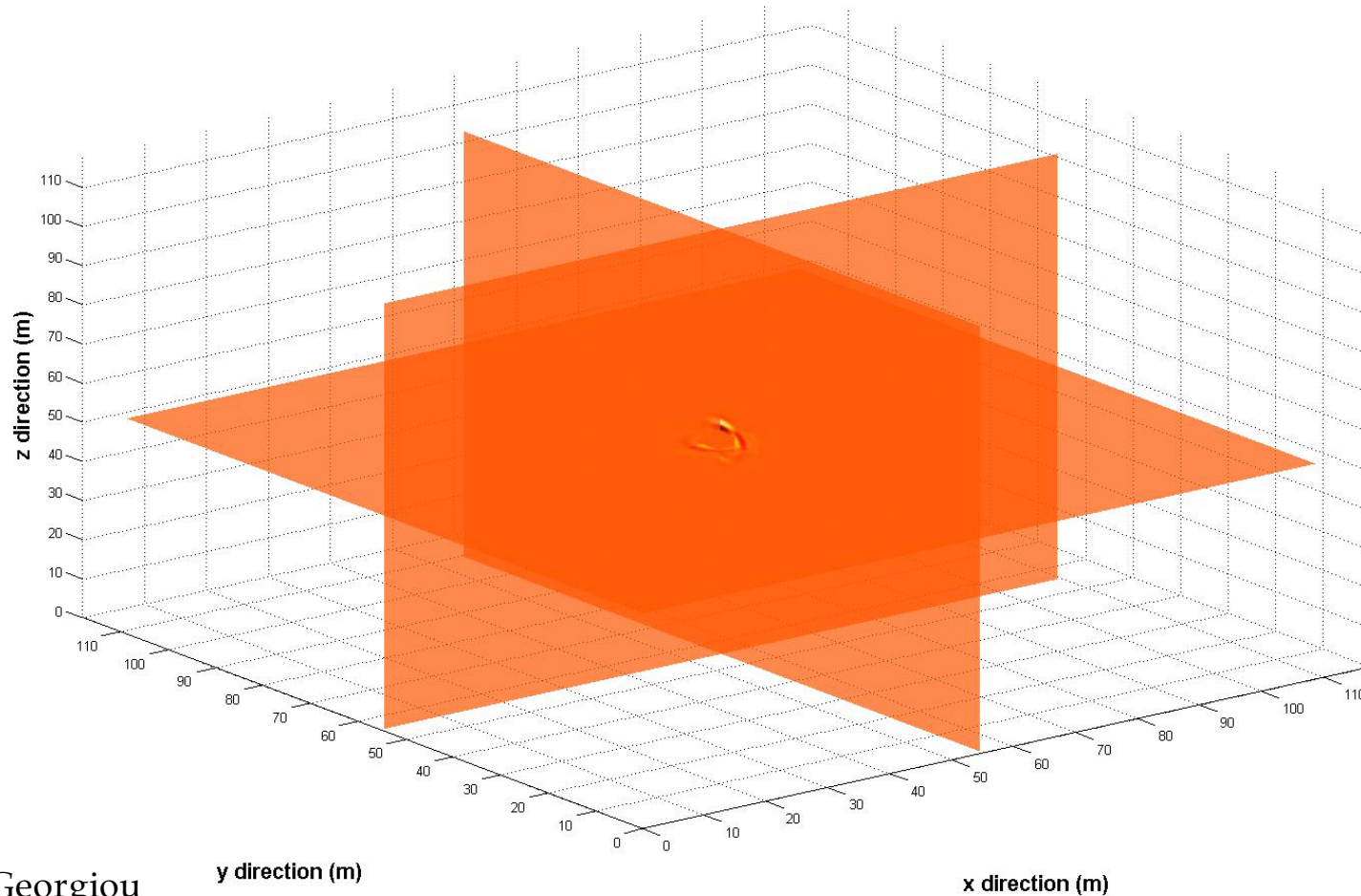


Fotis Georgiou



# Developments

## Source directivity method



Fotis Georgiou

y direction (m)

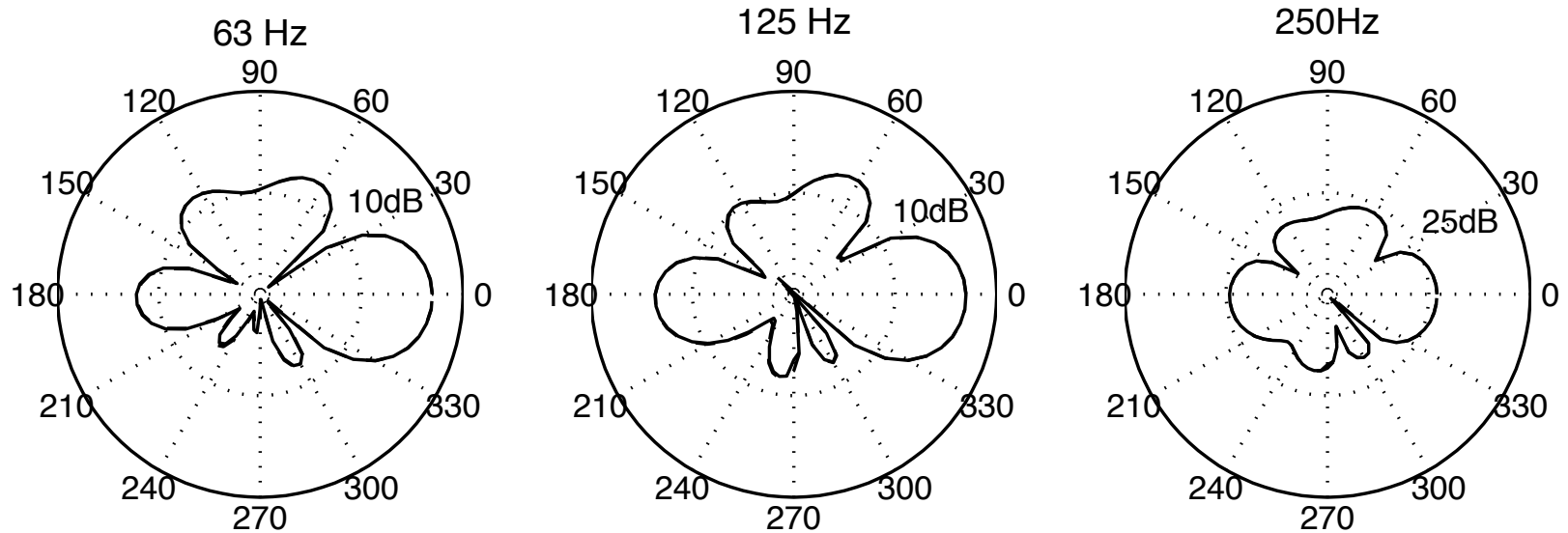
x direction (m)

Georgiou, F., Hornikx, M. (2014). Incorporating source directivity in the Pseudospectral time-domain method by using spherical harmonics. , J. Acoust. Soc. Am., Manuscript in preparation for submission.

Maarten Hornikx

# Developments

## Source directivity method



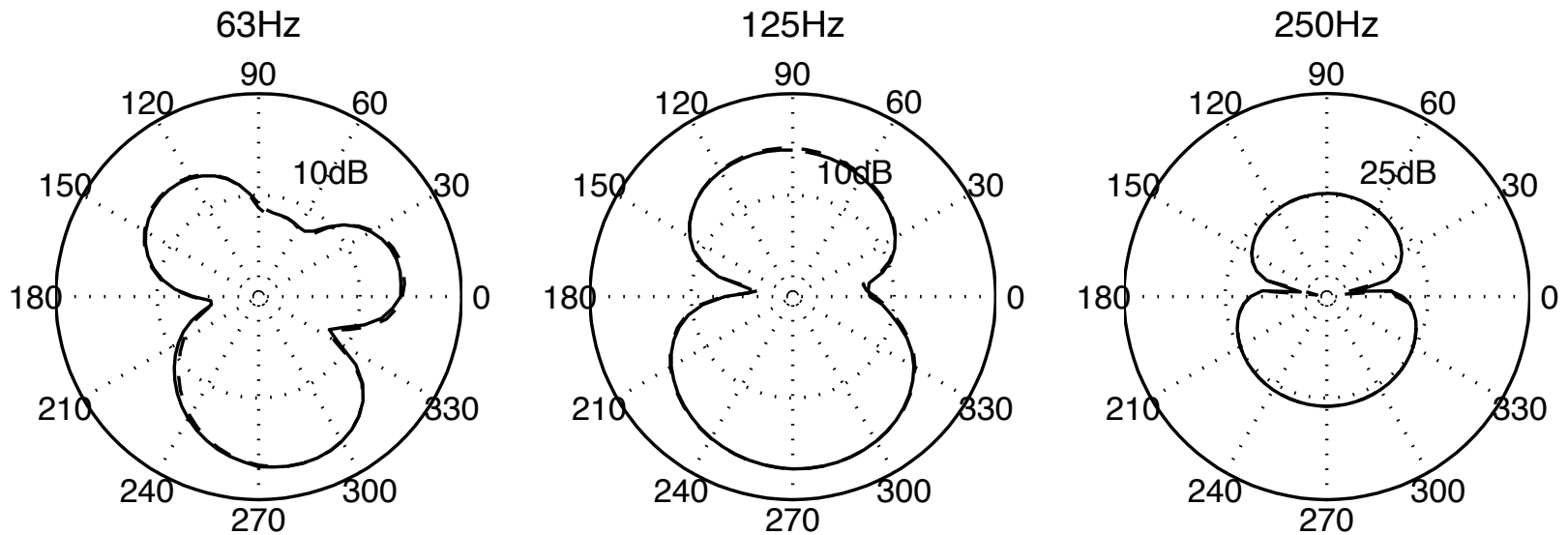
Vertical directivity

--- Original  
— Modeled

Fotis Georgiou

# Developments

## Source directivity method



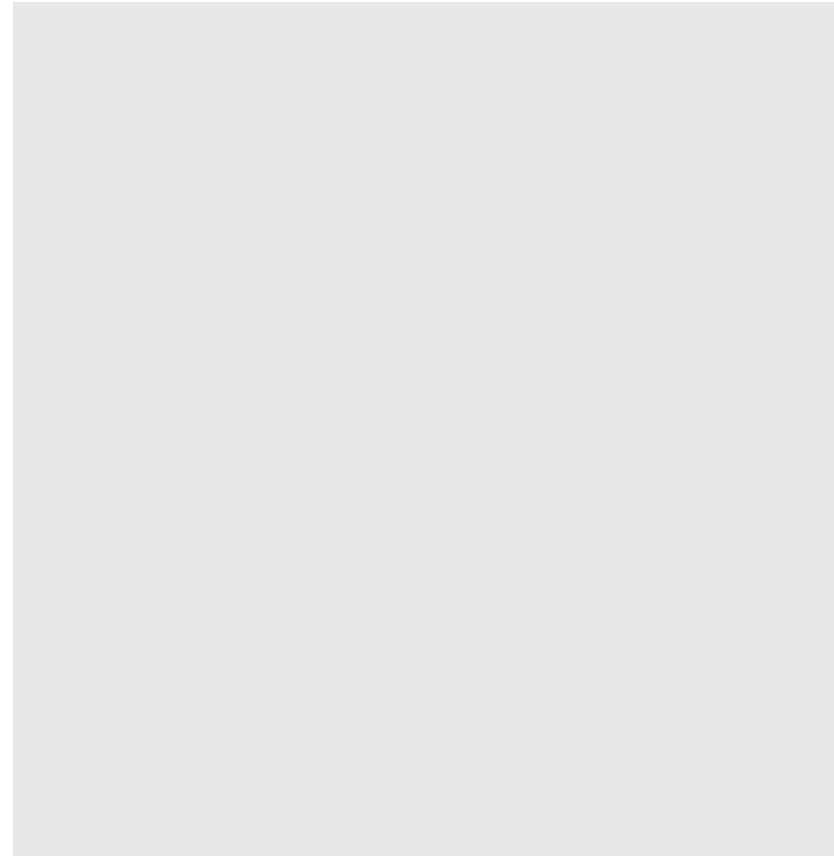
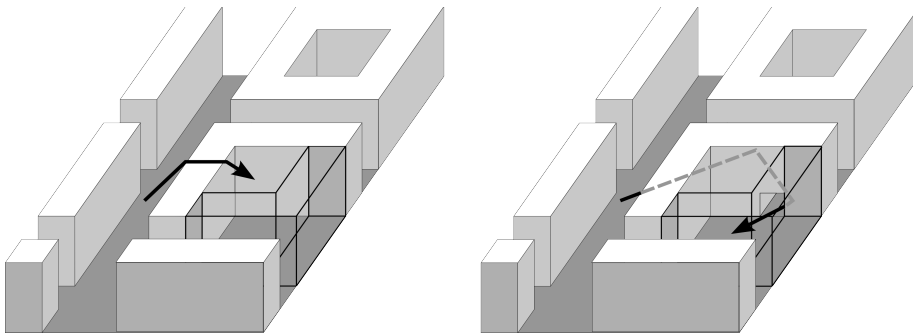
Horizontal directivity

--- Original  
— Modeled

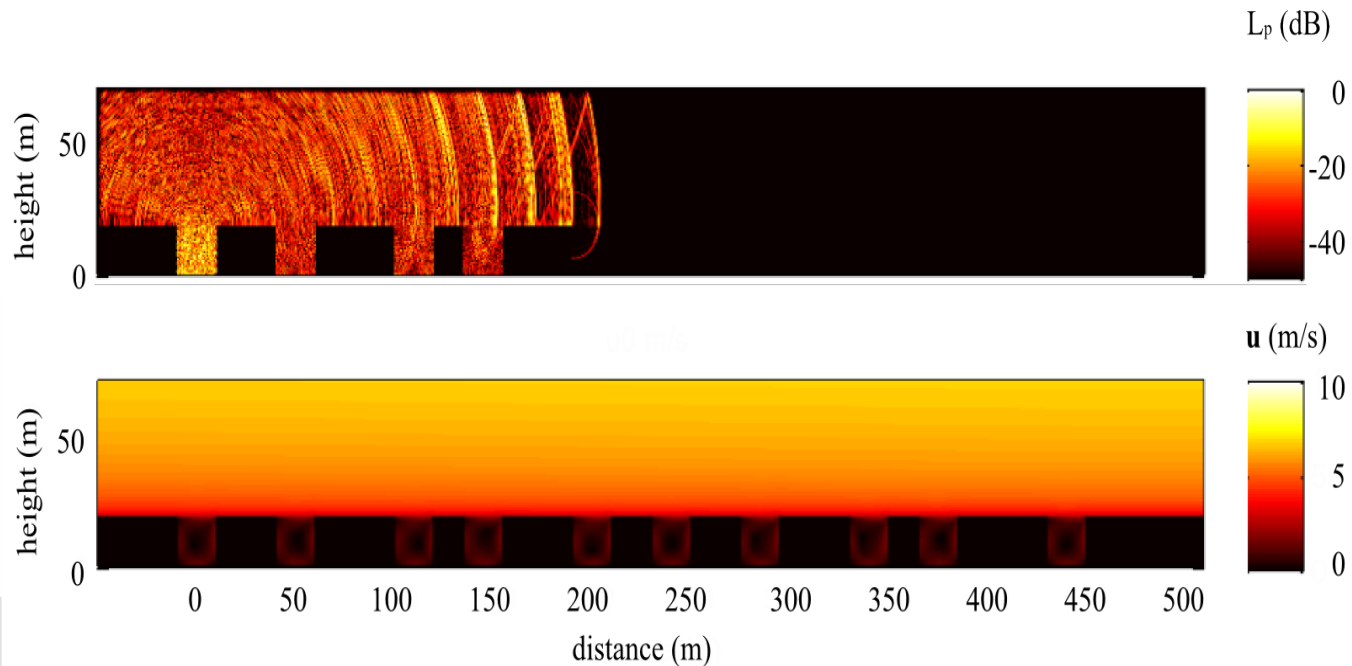
Fotis Georgiou

## 3D urban environments

### Openings to courtyards

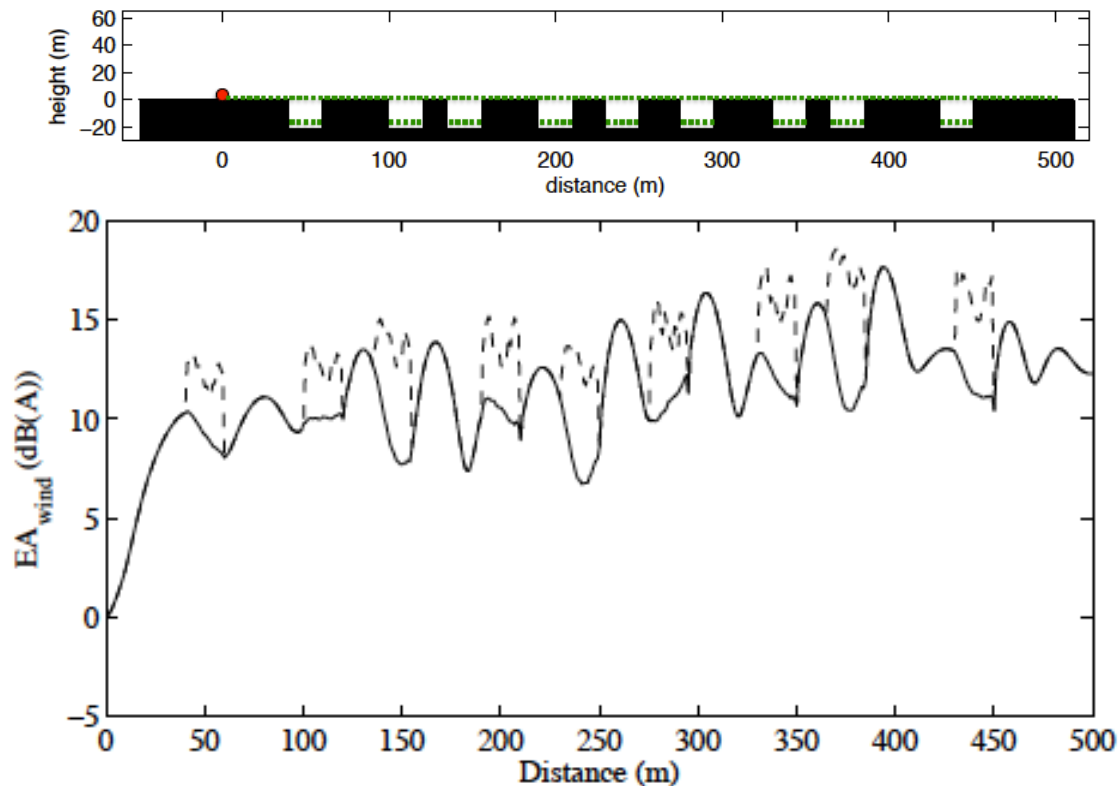


## Urban topology and wind



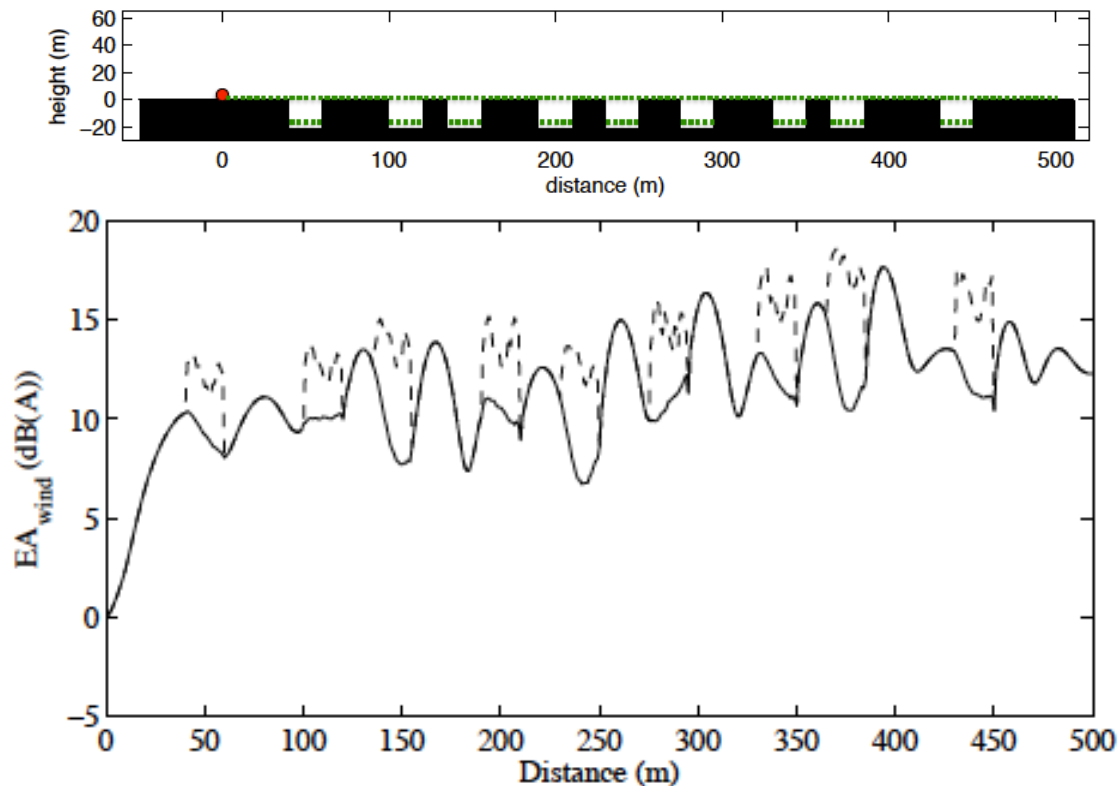
Karin Conen

## Urban topology and wind



Karin Conen

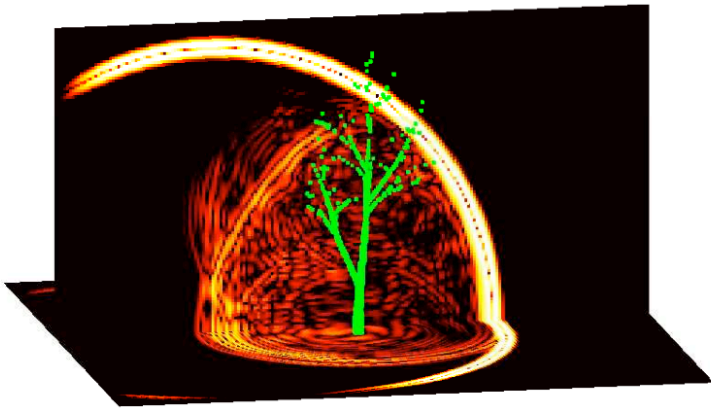
## Urban topology and wind



Karin Conen

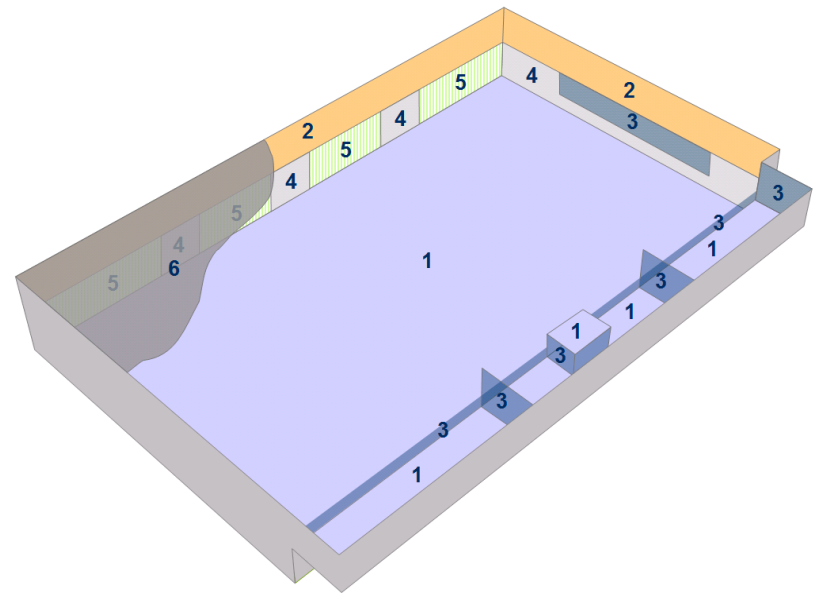
## Urban noise mitigation

- Green facades
- Green roofs
- Low height green barrier
- Trees
- Ground roughness

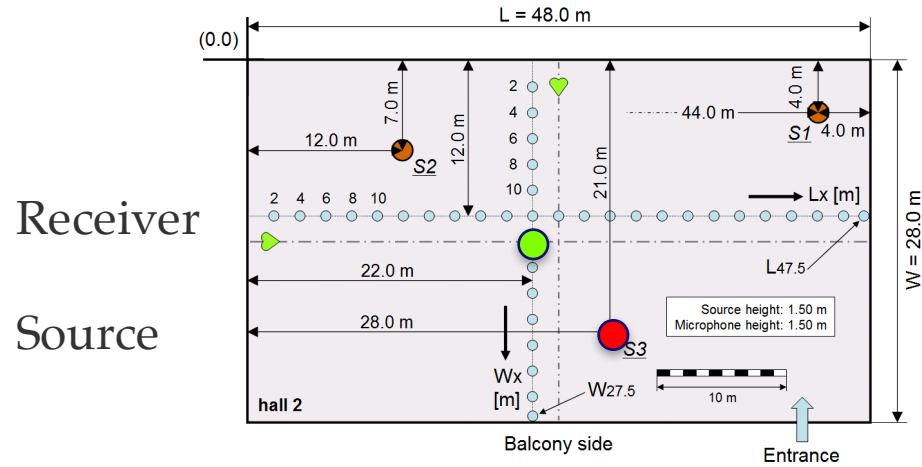




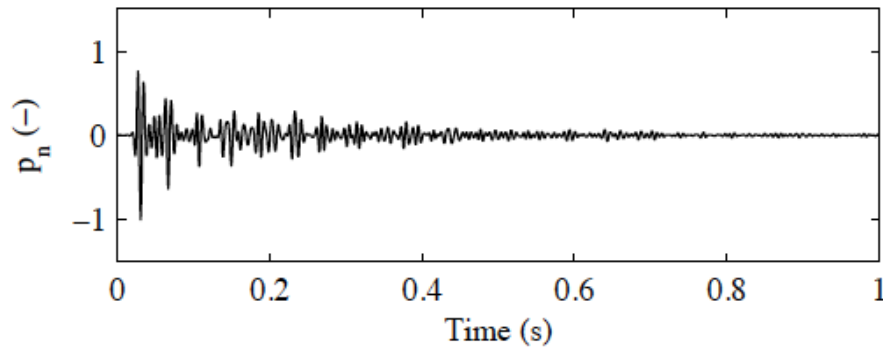
## Sports hall



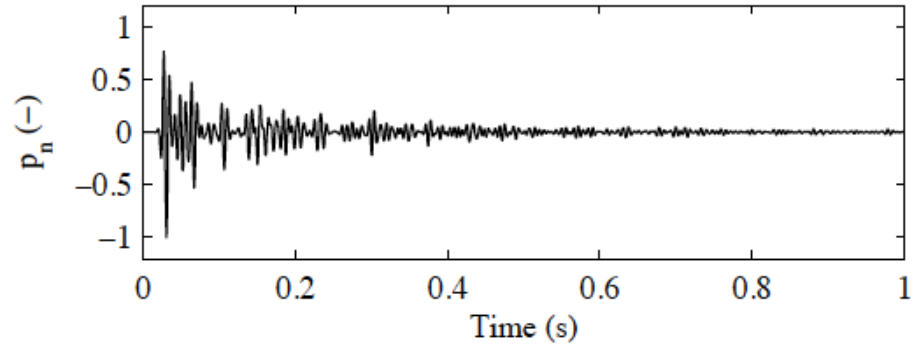
# Sports hall



# PSTD



Measured



Measured  
PSTD



## openPSTD

- New User Interface
- Implementation of recent developments
  - 3D implementation
  - Grid refinement
  - Meteorological effects
  - Source directivity
- Code Efficiency
  - Parts of code in C++
  - Including combined CPU/GPU acceleration

## Developments and Applications

- Further developments
  - Hybrid PSTD-DG method
  - Broadband impedance boundary conditions
  - Turbulence scattering
  - Include coupling with structural vibrations (building acoustics)
- Applications
  - Indoor and outdoor scenarios that need to be solved by a wave-based method
  - Auralization of environments

## Acknowledgements

- Raúl Pagan Munoz
- Fotis Georgiou
- Thomas Krijnen
- Louis van Harten
- Remy Wenmaekers
- Constant Hak
- Karin Conen
- Daan Steeghs
- Eef Brouns

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